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Let  $F(S, K, \sigma, r, T)$  be the price of a call option calculated using the Black-Scholes formula [1], where  $S$  is the current stock price,  $K$  is the strike price,  $T$  is the time to maturity of the option,  $r$  is the risk-free rate, and  $\sigma$  is the volatility. Let  $s(x)$  denote the logistic function. In the study, the efficiency of approximating  $F(S, K, \sigma, r, T)$  using neural networks of various architectures has been investigated. In particular, we constructed a feedforward one hidden layer artificial neural network of the form

$$G(\mathbf{x}) = (G_1(\mathbf{x}), G_2(\mathbf{x})), \text{ where } G_k(\mathbf{x}) = \left( \sum_{i=1}^{10} \alpha_i^k s(\mathbf{w}_i^k \cdot \mathbf{x} + \theta_i^k) + \beta_i^k \right), k = 1, 2;$$

$\mathbf{x} = \left( \frac{\log(S/K)}{\sigma\sqrt{T}}, \frac{r\sqrt{T}}{\sigma}, \sigma\sqrt{T} \right)$ , for which the following theorem is proven.

**Theorem 1.** Based on a test sample of size  $N = 2000$ , with a confidence level of 99.9%, it can be stated that for  $K = 1$  and

$$(S, \sigma, r, T) \in [0.5, 2] \times [0.1, 1.0] \times [0.0, 0.1] \times [0.1, 1.0]$$

the estimation  $|SG_1(\mathbf{x}) + Ke^{-rT}G_2(\mathbf{x}) - F(S, K, \sigma, r, T)| < 0.001$  holds with a probability of at least 0.998.

#### REFERENCES

- [1] F. Black, M. Scholes, The Pricing of Options and Corporate Liabilities, *Journal of Political Economy*, v. 81, pp. 637–654, 1973.

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