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About the heritability of uniformity of the *fractional part* of the convolution with a uniform random variable on a tessellation

In [1] the term fractional part was unified. In [2] it was shown that the fractional part of a convolution with a uniform on a square random variable is also uniform on a square. This work continues the generalization of these results.

Definition. A set $M \subset \mathbb{Z}^n$ is called **-connected* if each pair of dots from M can be connected by a polygonal chain which segments have unit length and which nodes are elements of M .

Theorem 1. Let $M \subset \mathbb{Z}^n$ be a finite and **-connected* set, and \mathbb{Z}^n can be tiled with M . Let $\xi \sim R\{M\}$, η be an independent with ξ integer n -dimensional random variable. Then $\{\xi + \eta\} \sim R\{M\}$.

Theorem 2. Let $M \subset \mathbb{R}^n$ be a bounded connected measurable set, and \mathbb{R}^n can be tiled with M . Let $\xi \sim R\{M\}$, η be an independent with ξ n -dimensional random variable. Then $\{\xi + \eta\} \sim R\{M\}$.

Л И Т Е Р А Т У Р А

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