

Gagarin Yu. E., Stepovich M. A. (Kaluga, Russia) — Interval estimation of the probability of error in the classification of objects with stochastic data.

To classify objects, we apply the Bayesian criterion, which provides the minimum level of error. We assume that there are no losses if the correct solution is chosen when observing a specific value x of the trait and losses are rare if the solution is incorrect. Under such conditions, the probability of classification error is determined by:

$$P(e) = 1 - \sum_{j=1}^M \int_{R_j} \eta_j(x, \Theta) dx,$$

where $\eta_j(x, \Theta) = P(x | \omega_j)P(\omega_j)$, Θ — vector of parameters; R_j — the area in the attribute space corresponding to ω_j the object; M — number of objects.

The values of attributes x_i , $i = \overline{1, n}$ are the results of specific experiments, and how any measurements contain random errors that need to be considered. The values of the functions $\eta_j(x, \Theta) \pm \Delta\eta_j(x, \Theta)$ will have an error $\Delta\eta_j(x, \Theta)$, taking into account which areas R_j will not be determined uniquely. More accurate is the formula that takes into account random errors of the source data:

$$P(e) \pm \Delta P(e) = 1 - \sum_{j=1}^M \int_{R_j \pm \Delta R_j} [\eta_j(x, \Theta) \pm \Delta\eta_j(x, \Theta)] dx.$$

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