

Zadorozhniy V. G. (Voronezh, Russia) **About the expectation of solution a linear system of differential equations with three random coefficients.**

Cauchy problem considered

$$\frac{dx}{dt} = \varepsilon_1(t)Ax + \varepsilon_2(t)x + \varepsilon_3(t)f(t), \quad (1)$$

$$x(t_0) = x_0. \quad (2)$$

Here $t \in \mathbb{R}, T = [t_0, t_1], x : \mathbb{R} \rightarrow \mathbb{R}^n$ is the desired vector function, $\varepsilon_1, \varepsilon_2$ is the Laplace random processes posed of characteristic functionals [1, стр. 30].

$$\varphi_j(u) = \frac{\exp(i \int_T \xi_j(s)u(s)ds)}{1 + \int_T \int_T b_j(s_1, s_2)u(s_1)u(s_2)ds_1ds_2}, j = 1, 2,$$

ε_3 is random processes, A is matrix of size $n \times n$, $f : T \rightarrow \mathbb{R}^n$ is given vector function, x_0 is random vector. Here $\xi_j(s) = M(\varepsilon_j(s))$ is the expectation of a random process ε_j , $b_j(s_1, s_2) = M(\varepsilon_j(s_1)\varepsilon_j(s_2)) - M(\varepsilon_j(s_1))M(\varepsilon_j(s_2))$ is the covariance function of a random process ε_j , $i = (-1)^{0,5}$, $u : T \rightarrow \mathbb{R}$ is a summable on T function.

Theorem. If the conditions are met

$$\|A\|^2 \int_T \int_T b_1(s_1, s_2)ds_1ds_2 < 1, \int_T \int_T b_2(s_1, s_2)ds_1ds_2 < 1,$$

$\varepsilon_1, \varepsilon_2, \varepsilon_3, x_0$ is independent und the functions ξ_j, b_j, f continuous on T , then

$$\begin{aligned} M(x(t)) = & \\ = \exp(A \int_{t_0}^t \xi_1(s)ds) \sum_{k=0}^{\infty} A^{2k} & \left(\int_{t_0}^t \int_{t_0}^t b_1(s_1, s_2)ds_1ds_2 \right)^k \frac{\exp(\int_{t_0}^t \xi_2(s)ds M(x_0))}{1 - \int_{t_0}^t \int_{t_0}^t b_2(s_1, s_2)ds_1ds_2} + \\ + \int_{t_0}^t \exp(A \int_s^t \xi_1(\tau)d\tau) \sum_{k=0}^{\infty} & A^{2k} \left(\int_s^t \int_s^t b_1(s_1, s_2)ds_1ds_2 \right)^k \times \\ \times \frac{\exp(\int_s^t \xi_2(\tau)d\tau)}{1 - \int_s^t \int_s^t b_2(s_1, s_2)ds_1ds_2} & M(\varepsilon_3(s))f(s)ds \end{aligned}$$

is the expectation of solution of problem (1), (2).

Note that the case when $T = [0, \infty)$. The system (1) is asymptotically stable on average [2] if

$$\left\| \exp(A \int_{t_0}^t \xi_1(s)ds) \sum_{k=0}^{\infty} A^{2k} \left(\int_{t_0}^t \int_{t_0}^t b_1(s_1, s_2)ds_1ds_2 \right)^k \right\| \frac{\exp(\int_{t_0}^t \xi_2(s)ds)}{1 - \int_{t_0}^t \int_{t_0}^t b_2(s_1, s_2)ds_1ds_2} \rightarrow 0$$

with $t \rightarrow \infty$.

СПИСОК ЛИТЕРАТУРЫ

1. *Zadorozhniy V.G.* Methods of variational analysis. Moscow - Izhevsk, RKhD, - 2006.
2. *Zadorozhniy V.G.* Stabilization of linear systems by a multiplicative random noise. Differential equations, 2018, Vol. 54, No. 6, pp. 728-747.